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INTERNATIONAL CONFERENCE ON RESEARCH, IMPLEMENTATION AND EDUCATION OF MATHEMATICS AND SCIENCES 2014

ICRIEMS 2014

Yogyakarta, 18-20 May 2014

Global Trends and Issues on Mathematics and Sciences and the Education

PROCEEDING

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Conference Proceedings

INTERNATIONAL CONFERENCE ON RESEARCH, IMPLEMENTATION AND EDUCATION OF MATHEMATICS AND SCIENCES (ICRIEMS) 2014

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Global Trends and Issues
on Mathematics and Science
and The Education

Faculty of Mathematics and Natural Sciences
Yogyakarta State University

ICRIEMS 2014 : Global Trends and Issues on Mathematics and Science and The Education

- Mathematics & Mathematics Education
- Physics & Physics Education
- Chemistry & Chemistry Education
- Biology & Biology Education
- Science Education

Preface

Bless upon God Almighty such that this proceeding on International Conference on Research, Implementation, and Education of Mathematics and Sciences (ICRIEMS) 2014 may be compiled according to the schedule provided by the organizing committee. All of the articles in this proceeding are obtained by selection process by the reviwer team and already ben presented in the Conference on 18 – 20 May 2014 in the Faculty of Mathematics and Natural Sciences, Yogyakarta State University. This proceeding consists of 344 parallel papers, and comprises 9 fields, that is mathematics, mathematics education, physics, physics education, chemistry, chemistry education, biology, biology education, and science education.

The theme of ICRIEMS 2014 is 'Global Trends and Issues of Mathematics and Science and the Education'. The main articles in this conference are given by five keynote speakers, which are Prof. Dean Zollman (Physics Department, Kansas State University), Prof. David F. Treagust (Center of Education, Curtin University), Prof. Dr. Amy Cutter-Mackenzie (School of Education, Southern Cross University, Australia), Prof. Tran Vui (Hue University, Vietnam), and Asst. Prof. Dr. Duangjai Nacapricha (Faculty of Science, Mahidol University). The conference is also supported by the LPTK (Lembaga Pendidikan Tenaga Kependidikan) Forum from Faculty of Mathematics and Sciences that consists of 12 universities all over Indonesia. Each member of the Forum contributed one invited speakers, such that there are an additional 10 invited speakers presenting in the forum. Besides the keynote and invited speakers, there are also 344 parallel articles that presented the latest research results in the field of mathematics and sciences, and the education. These parallel session speakers come from researchers from Indonesia and abroad, including Malaysia and Australia.

Hopefully, this proceeding may contribute in disseminating research results and studies in the field of Mathematics and Sciences and the Education such that they are accessible by many people and useful for the Nation Building.

Yogyakarta, June 2014

The Editor Team

Forewords from The Head of Committee

Assalamu'alaikum wa Rahmatullahi wa Barakatuh
May God bless upon us.

Your excellency The president of UNY Prof. Dr. Rochmat Wahab, M. Pd., M.A., ladies and gentlemen, good morning and welcome to State University Yogyakarta. This seminar entitled International Conference on Research, Implementation, and Education of Mathematics and Science (ICRIEMS): global trends and issues on mathematics and science and the education is organized by the Faculty of Mathematics and Science, State University of Yogyakarta working together with 12 members of the Association of the Faculty of Math and Sciences from Teacher Education Program (LPTK). This seminar is also dedicated to the golden aniversary of UNY; 1 among 90 academic activities dedicated to the aniversary.

Ladies and gentlemen, on behalf of the committee of this conference, I would like to express highest appreciation and gratitudes to the keynote speakers, including:

1. Prof. David F. Treagust (Center of Science Education Curtin University)
2. Prof. Dean Zollman (Physics Dept, Kansas University, US)
3. Dr. Amy Cutter-Mackenzie (School of Education, Southern Cross University, Australia)
4. Asst. Prof. Dr. Duangjai Nacapricha (Faculty of Science , Mahidol University)
5. Prof. Tran Vui (College of Education, Hue University, Hue City, Vietnam)

Secondly, I would like also to give sincere thanks and gratitudes to the speakers from 10 College of Educations, including:

1. Universitas Negeri Surabaya (UNESA): Prof. Dr. Muchlas Samani, and 33 speakers
2. Universitas Negeri Jakarta (UNJ): Prof. Dr. Gerardus Pola, and 7 speaker
3. Universitas Pendidikan Indonesia (UPI): Dr. Hary Firman, and
4. Universitas Negeri Malang (UM): Prof. Effendi, Ph.D
5. Universitas Negeri Padang (UNP): Prof. Tjeerd Plomp
6. Universitas Negeri Semarang (UNNES): Prof. Dr. Supriyadi Rustad

7. Universitas Pendidikan Singaraja (UNDIKSA): Prof. Dr. I Nengah Suparta, M.Si
8. Universitas Negeri Makasar (UNM): Oslan Junaidi, Ph.D
9. Universitas Negeri Gorontalo (UNG): Prof. Dr. Sarson Pomalto, M.Pd
10. Universitas Negeri Yogyakarta (UNY): Dr. Jaslin Ikhsan

Next, I also would like to thanks to our special guests and speakers from:
1. Universitas Pendidikan Sultan Indris (UPSI), Malaysia
2. University of Mahidol, Thailand
3. University of Malaysia in Trengganu

Next, I would like to thanks and welcome to 379 speakers from the entire Indonesia and all participants registered in this seminar.

Ladies and gentlemen, recently the number of research and publication on mathematics and science and the education is vulnarable. It is nescessary for us to organise, to share, and to publish the results of the research in this conference. I hope the conference will bear fruitful results and promote networking and future collaborations for all participants from diverse background of expertise, intitutions, and countries to promote science, mathematics, and the education.

Finally, I am delighted to thank the committee members who have been working very hard to ensure the succes of the conference.

Please enjoy the conference and enjoy Yogyakarta, the city of education, tourism, and culture. Thank you very much.

Assalamu'alaikum wa rahmatullahi wa barrakatuh

Dr. Slamet Suyanto, M. Ed.

Forewords from The Dean of Faculty of Mathematics and Natural Sciences, Yogyakarta State University

Assalamu'alaikum warahmatullahi wabarakatuh

May peace and God's blessings be upon us all.

On behalf of the Organizing Committee, first of all allow me to extend my warmest greeting and welcome to the International Conference on Research, Implementation, and Education of Mathematics and Sciences 2014, held in Yogyakarta State University, one of the qualified education universities in Indonesia.

To celebrate the 50th Commemoration of Yogyakarta State University, our faculty, in collaboration with Forum of MIPA LPTK, has the opportunity to conduct International Conference on Research, Implementation, and Education of Mathematics and Sciences 2014. This conference proudly presents five keynote speeches by five fabulous speakers: Prof. Dean Zollman, Prof. David F. Treagust, Prof. Dr. Amy Cutter-Mackenzie, Prof. Tran Vui, and Asst. Prof. Dr. Duangjai Nacapricha, around 380 parallel speakers with 344 orally presented articles.

Distinguished guest, ladies and gentlemen,

The independence of a country is impossible to gain if the education does not become the priority and it is not supported with the development of technology. We all know that the technology development could be achieved if it is supported by the improvement of firm fundamental knowledge. The empowerment of fundamental knowledge could not be separated from research which is related to the development of technology and the learning process in school and universities.

This conference is aimed to pull together researchers, educators, policy makers, and practitioners to share their critical thinking and research outcomes. Therefore, we are able to understand and examine the development of fundamental principle, knowledge, and technology. By perceiving the matters and condition in research and education field of mathematics and sciences, we could take a part in conducting qualified education to reach out the real independence of our nation.

Distinguished guest, ladies, and gentlemen

This conference will be far from success and we could not accomplish what we do without the support from various parties. So let me extend my deepest gratitude and highest appreciation to all committee members. I would also like to thank each of participants for

attending our conference and bringing your expertise to our gathering. Should you find any inconveniences and shortcomings, please accept my sincere apologies.

To conclude, let me wish you fruitful discussion and a very pleasant stay in Yogyakarta.

Wa'alaikumsalam warahmatullahi wabarakatuh

Dr. Hartono

Table of Content

PHYSICS

PHYSICS EDUCATION

BIOLOGY

BIOLOGY EDUCATION

CHEMISTRY

SCIENCE EDUCATION

RANDOM EFFECT MODEL AND GENERALIZED ESTIMATING EQUATIONS FOR BINARY PANEL RESPONSE

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Abstract

Panel data models are widely used in empirical analysis because they allow researchers to control for unobserved individual time-invariant characteristics. However, these models pose important technical challenges. In particular, if individual heterogeneity is left completely unrestricted, and then estimates of model parameters in nonlinear and/or dynamic models suffer from the incidental parameters problem. This problem arises because the unobserved individual characteristics are replaced by inconsistent sample estimates, which, in turn, biases estimates of model parameters. Logit model or probit model on panel data with using univariate approximation (neglect correlation) result consistent estimator but not efficient. In many cases, data are multivariate or correlated (e.g., due to repeated observations on a study subject or for subjects within centers) and it is appealing to have a model that maintains a marginal logistic regression interpretation for the individual outcomes.

In this paper, we studied modeling binary panel response using Random Effects Model (REM). Using Monte Carlo Simulation, we research correlations effects to maximum likelihood estimator (MLE) of random effects model. We also compare MLE of REM to Generalized Estimating Equations (GEE) of logit model. Data were generated by using software R.2.8.1 as well as the estimation on the parameters. Based on the result, it can be concluded that (a) In some value of individual effect, random effects model is more better GEE. (b) REM can be accommodating individual effects and closer to parameter than the other. (c) REM is appropriate method to estimate covarians of utility at individual effect having value about one.

Keywords : Random Utility Models, Maximum Likelihood Estimator Generalized Estimating Equations, Logit Models, Probit Models

1. Introduction

Panel data models are widely used in empirical analysis because they allow researchers to control for unobserved individual time-invariant characteristics. However, these models pose important technical challenges. In particular, if individual heterogeneity is left completely unrestricted then estimates of model parameters in nonlinear and/or dynamic models suffer from the incidental parameters problem. This problem arises because the unobserved individual characteristics are replaced by inconsistent sample estimates, which, in turn, biases estimates of model parameters (Greene, 2003). Liang and Zeger (1986), shown that Logit model or Probit

model on panel data with using univariate approximation (neglect correlation) result consistent estimator but not efficient. In many cases, data are multivariate or correlated (e.g., due to repeated observations on a study subject or for subjects within centers) and it is appealing to have a model that maintains a marginal logistic regression interpretation for the individual outcomes. Commonly used logistic random effects models do not have this property, since the logistic structure is lost in integrating out the random effects. An alternative is to use a marginal analysis that avoids complete specification of the likelihood (Liang and Zeger, 1986; Prentice, 1988; Lipsitz *et al.*). Prentice (1988) proposed modeling strategic by GEE to obtain consistent estimator and normal asymptotic. GEE are hindered multiple integral by marginal distribution.

Nugraha *et al.*(2008) have tested Logit Model in multivariate binary response using Monte Carlo simulation. They concluded that GEE more proper on height correlation, although estimators of correlation was underestimated. MLE of Probit Model could not derive by analytic, because the likelihood functions formed a multiple integral. Simulation approximation to compute multiple integral caused bias. The others problem on Probit Model are the log likelihood function not global concave, so there are no one solutions. Simulation methods rely on approximating an integral (that does not have a closed form) through Monte Carlo integration. Draws are taken from the underlying distribution of the random variable of integration and used to calculate the numeric integral. Simulated maximum log likelihood estimation is a common estimator used for Probit Model and random effects model. Such estimators exhibit a non-negligible bias when too few draws are used in estimation, and prior research exists regarding the magnitude and properties of this bias with respect to quasi-random draws (Bhat, 2001). Train (1999) provide further evidence of the benefits of intelegent drawing techniques such as Halton and Shuffled Halton, which require fewer numbers of draws than pseudo-random in order to uncover identification issues.

In this paper, we studied modeling binary panel response using random effects model. Using Monte Carlo Simulation, we research correlations effects to maximum likelihood estimator (MLE) of Random Effects model. We also compare MLE on Random Effects model to GEE on Logit Model.

2. GEE Model

In the panel response within exponential family distribution, Liang dan Zeger (1986) proposed the GEE model. For the binary response ($Y_{i1},...,Y_{iT}$) with each Y_{it} binary value (dichotomous), both link logit and link probit can be utilized for GEE model. Contoyannis et al. (2001) has been constructed probit model on binary panel data by the model of :

$$Y_{it} = \beta' X_{it} + \xi_i + \varepsilon_{it} \quad \text{for } i=1,...,n \text{ and } t=1,...,T \qquad \textbf{(1)}$$

ξ_i is individual effect within the normal distribution and mean value of null and the variance of σ_η^2. Whereas $\varepsilon_{it} \sim N(0, \sigma^2)$ and independent with ξ_i. X_{it} are vector px1 respect to the independent variable for responden i on t periode. β is a parameter vector in px1 size. Individual probability i for making a decision series was calculated by using conditional probability.

We assume that each of n individual observed T times. Y_{it} is t^{nd} response on i^{nd} individual/subject and each response are binary. So, response for i^{nd} individual can be

$$Y_i = (Y_{i1},....,Y_{iT})$$

that is vector 1xT. $Y_{it} = 1$ if i^{nd} subject and t^{nd} response choose the first alternative and $Y_{it} = 0$ if choose the second alternative. Each subject have covariate X_i (individual characteristic) dan covariate Z_{ijt} (characteristic of alternative j=0,1). To simplify, we choose one of individual characteristic and one of characteristic of alternative. Utility of subject i choose alternative j on response t is

$$U_{ijt} = V_{ijt} + \varepsilon_{ijt}. \quad \text{for } t=1,2,...,T \text{ ; } i=1,2,...,n \text{ ; } j=0,1 \qquad (2)$$

with $V_{ijt} = \beta 0_{jt} + \beta_{jt}X_i + \gamma_t Z_{ijt}$.

By assumption that decision makers choosing alternative based on maximum utility, model can be represented in different of utility,

$$U_{it} = V_{it} + \varepsilon_{it} \qquad (3)$$

with $V_{it} = (V_{i1t} - V_{i0t})$ and $\varepsilon_{it} = (\varepsilon_{i1t} - \varepsilon_{i0t})$.

Expectation of eq. (3) are

$E(\varepsilon_{it}) = E(\varepsilon_{i1t}) - E(\varepsilon_{i0t}) = 0.5772 - 0.5772 = 0$

$E(\alpha_i) = 0$; $E(U_{it}) = V_{it}$

and theirs varians are

$$Var(\varepsilon_{it}) = Var(\varepsilon_{i1t}) + Var(\varepsilon_{i0t}) = \frac{\pi^2}{6} + \frac{\pi^2}{6} = \frac{\pi^2}{3}$$

$$Var(\alpha_i) = Var(\alpha_{i0}) + Var(\alpha_{i1}) = 2\sigma^2$$

$$Var(U_{it}) = Var(\alpha_i) + Var(\varepsilon_{it}) = 2\sigma^2 + \frac{\pi^2}{3}$$

Covariance and Correlation among utilities are

$Cov(U_{it};U_{is}) = Cov((\alpha_i + \varepsilon_{it}), (\alpha_i + \varepsilon_{is})) = 2\sigma^2$ for all $t \neq s$

$$Cor(U_{it};U_{is}) = \frac{2\sigma^2}{\left(2\sigma^2 + \frac{\pi^2}{3}\right)}$$

Probability of subject i choose ($y_{i1} = 1,...., y_{iT} = 1$) is

$$P(y_{i1} = 1,...., y_{iT} = 1) = \int_{\varepsilon i} I(-V_{it} < \varepsilon_{it}).\, f(\varepsilon_i) d\varepsilon_i \qquad \forall t \qquad (4)$$

This probability value is multiple integral and depending on parameters β, γ and distribution of ε (Train, 2003).

The logit model can be derived by assumption that ε_{ijt} have Extreme Value Type I distribution (Gumbel) and independence each other (all i, j and t). Probability of subject i choose j=1 for response t^{nd} is

$$P(y_{it} = 1) = \pi_{it} = \frac{\exp(V_{i1t})}{[\exp(V_{i0t}) + \exp(V_{i1t})]} = \frac{\exp(V_{it})}{[1 + \exp(V_{it})]} \qquad (5)$$

with

$$V_{ijt} = \beta 0_{jt} + \beta_{jt}X_i + \gamma_t Z_{ijt} \quad \text{for } t=1,2,...,T \text{ ; } i=1,2,...,n \text{ ; } j=0,1.$$

On Logit Model, GEE are easier to implement than MLE. GEE use approximation by marginal distribution and can be represented by

$$G(\theta) = \sum_{i=1}^{n} W_i \Delta_i S_i^{-1} (Y'_i - \pi'_i) = 0 \qquad (6)$$

with $W_i = diag\begin{pmatrix} 1 & & 1 \\ X_i & .... & X_i \\ (Z_{i11} - Z_{i01}) & & (Z_{i1T} - Z_{i0T}) \end{pmatrix}$; $\Delta_i = diag\left(\pi_{i1}(1-\pi_{i1}) \quad ... \quad \pi_{iT}(1-\pi_{iT})\right)$

$$S_i = A_i^{1/2} R_i A_i^{1/2} \text{ with } A_i^{1/2} = \begin{pmatrix} \sqrt{Var(Y_{i1})} & \dots & 0 \\ \dots & \dots & \dots \\ 0 & \dots & \sqrt{Var(Y_{iT})} \end{pmatrix}$$

with $Y_i = (Y_{i1},....,Y_{iT})$; $\pi_i = (\pi_{i1},...., \pi_{iT})$. Estimators GEE are solving equations (6) on sample data W (Nugraha et al., 2008) .

GEE on Probit Model are solving of estimating equation

$$G(\theta) = \sum_{i=1}^{n} W_i \Delta_i S_i^{-1} (Y'_i - \pi'_i) = 0 \tag{7}$$

with $\pi_{it} = \Phi(V_{it})$; $\Delta_i = diag(\phi(V_{it}))$. Estimations of parameter correlations are underestimated. GEE on probit model are equivalent to GEE on Logit Model.

3. Random Effects Model

From the equation of utility difference (3), we added the individual effect α_i

$$U_{it} = V_{it} + \alpha_i + \varepsilon_{it} \tag{8}$$

α_i is effect of individual i having normal distribution, $\alpha_i \sim NID(0, \sigma^2)$ and independent to ε_{it}. ε_{it} have Extreme Value Distribution.

Based on equation (8), we will estimate parameters (σ, β_t, γ_t) for t=1,..,T. By equation (5), we have conditional probability :

$$g_{it} = P(y_{it} = 1|\alpha_i) = P(\varepsilon_{it} < -V_{it}|\alpha_i) = \pi_{it} \mid \alpha_i = \frac{\exp(V_{it} + \alpha_i)}{[1 + \exp(V_{it} + \alpha_i)]}$$

$$= \frac{\exp(V_{it} + \alpha_i)}{[1 + \exp(V_{it} + \alpha_i)]} \tag{9}$$

Marginal probabilities from equation (4) for Random Effect Model are

$$P(y_{it} = 1) = \pi_{it} = \int_{-\infty}^{\infty} P(y_{it} \mid \alpha_i) f(\alpha_i) d\alpha_i$$

$$= \int_{-\infty}^{\infty} \frac{\exp(V_{it} + \alpha_i)}{[1 + \exp(V_{it} + \alpha_i)]} \phi(\alpha_i) d\alpha_i \tag{10}$$

$\phi(\xi_{it})$ is standard normal density.

$$P(y_{i1} = 1, \dots, y_{iT} = 1) = \int_{-\infty}^{\infty} \prod_{t=1}^{T} P(y_{it} \mid \alpha_i) f(\alpha_i) d\alpha_i$$

$$= \int_{-\infty}^{\infty} \prod_{t=1}^{T} \frac{\exp(V_{it} + \alpha_i)}{[1 + \exp(V_{it} + \alpha_i)]} \phi(\alpha_i) d\alpha_i \tag{11}$$

So,

$$P(y_{i1}, \dots, y_{iT}) = \int_{-\infty}^{\infty} \prod_{t=1}^{T} \left(\frac{\exp(V_{it} + \alpha_i)}{[1 + \exp(V_{it} + \alpha_i)]} \right)^{y_{it}} \left(1 - \frac{\exp(V_{it} + \alpha_i)}{[1 + \exp(V_{it} + \alpha_i)]} \right)^{1 - y_{it}} \phi(\alpha_i) d\alpha_i$$

MLE of parameters (β_t, γ_t ;σ), t=1,..T, can be obtained from likelihood function :

$$L(\beta,\gamma,\sigma)=\prod_{i=1}^{n}\int_{-\infty}^{\infty}\left(\prod_{t=1}^{T}(g_{it})^{y_{it}}(1-g_{it})^{1-y_{it}}\right)\phi(\alpha_i)\partial\alpha_i \tag{12}$$

Then the log-likelihood function is

$$LL=\log L(\beta,\gamma,\sigma)=\sum_{i=1}^{n}\log\left(\int_{-\infty}^{\infty}\prod_{t=1}^{T}\left((g_{it})^{y_{it}}(1-g_{it})^{1-y_{it}}\phi(\alpha_i)\right)\partial\alpha_i\right) \tag{13}$$

There are some methods of iteration to get the solution of equatian (13) : Newton-Raphson methods, BFGS methods, etc.

4. Generating Data Simulation and Result

We will generate simulation data with T=3, n=1000. Then, the equations of utility are

$U_{i0t} = \alpha_{i0} + \beta 0_{0t} + \beta_{0t}X_i + \gamma_t Z_{i0t} + \varepsilon_{i01}$ and

$$U_{i1t} = \alpha_{i1} + \beta 0_{1t} + \beta_{1t}X_i + \gamma_t Z_{i1t} + \varepsilon_{i11} \tag{14}$$

for i=1,...,N; j=0,1 and t=1,...,3; ε_{ijt} ~Extreme Value Type I, $\alpha_i \sim N(0,\sigma^2)$.

Equation (14) can be presented in difference of utility $U_{it} = U_{i1t} - U_{i0t}$. On Logit Model, equations of utility difference are

$$U_{it} = \beta 0_t + \beta_t X_i + \gamma_t Z_{it} + \alpha_i + \varepsilon_{it} \tag{15}$$

or

$U_{i1} = V_{i1} + \alpha_i + \varepsilon_{i1}$; $U_{i2} = V_{i2} + \alpha_i + \varepsilon_{i2}$;$U_{i3} = V_{i3} + \alpha_i + \varepsilon_{i3}$

with

$V_{it} = (V_{i1t} - V_{i0t}) = \beta 0_t + \beta_t X_i + \gamma_t Z_{it}$.

$Z_{it} = (Z_{i1t} - Z_{i0t})$; $\beta 0_t = \beta 0_{0t} - \beta 0_{1t}$;$\beta_t = \beta_{0t} - \beta_{1t}$; $\alpha_i = (\alpha_{i1} - \alpha_{i0})$.

We generate data on $\beta 0_t$ =-1; β_t = 0.5 , γ_t=0.3 and some of variance σ^2 =0; 0.5; 1; 2; 4, 6 using program R.2.8.1. From the data simulation, we built the Logit Model using three approximations. First, we assume independence each other for all i, j and t (independent logit model) and estimate parameters using MLE (θ_{MLECS}) . Second, we estimate parameter using GEE (θ_{GEE}). The last approximation is Random Effect Model using MLE (θ_{MLERE}). Results of the simulations presented in Figure 1 to Figure 10.

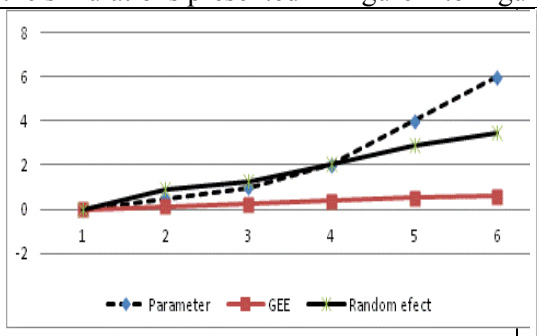

Figure 1. Estimator of σ^2

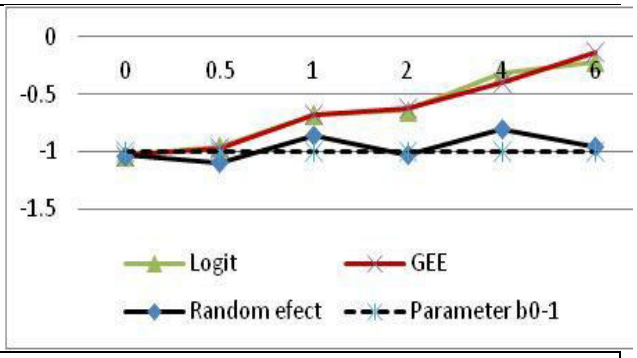

Figure 2. Estimator of $\beta 0_1$

Based on simulation result representing at Figure 1., estimator of σ^2 using Random effect Model (θ_{MLERE}) more accurate than GEE (θ_{GEE}). θ_{MLERE} have value closer to real value of parameter than θ_{GEE}.

Overall, estimator of $\beta 0_t$, β_t and γ_t in MLE as same as GEE (see Figure 2 to Figure 10).

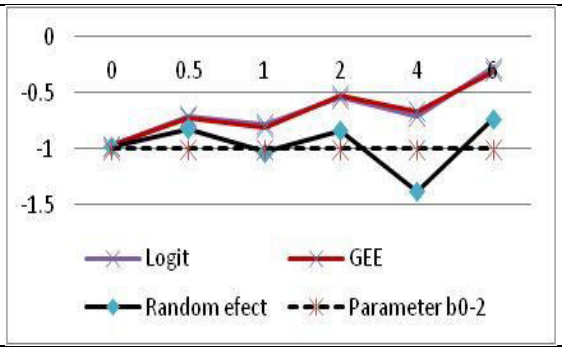

Figure 3. Estimator of $\beta 0_2$

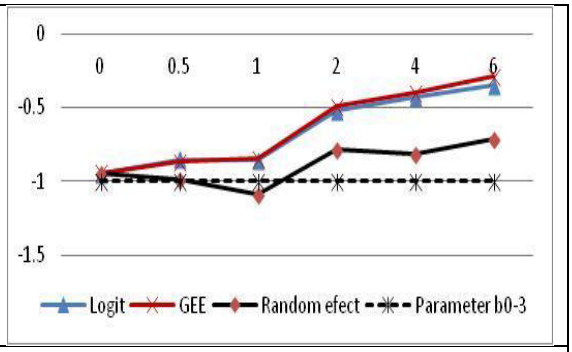

Figure 4. Estimator of $\beta 0_3$

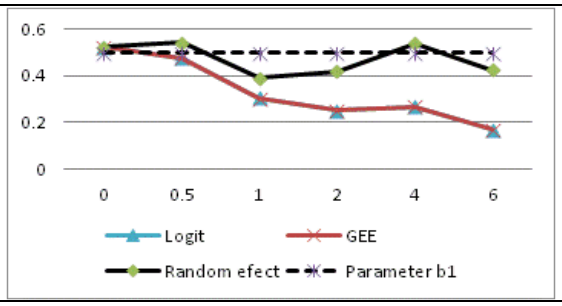

Figure 5. Estimator of β_1

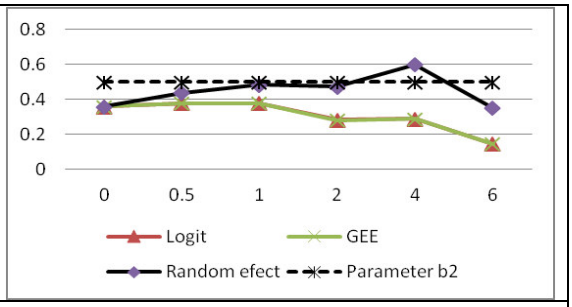

Figure 6. Estimator of β_2

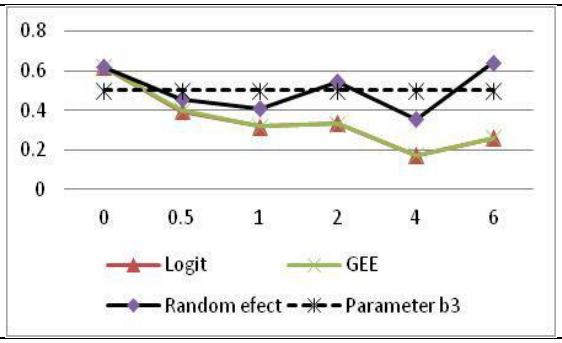

Figure 7. Estimator of β_3

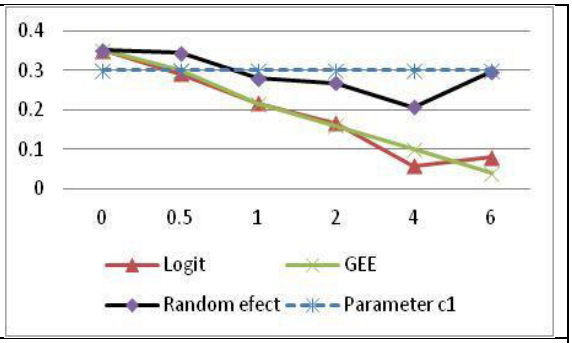

Figure 8. Estimator of γ_1

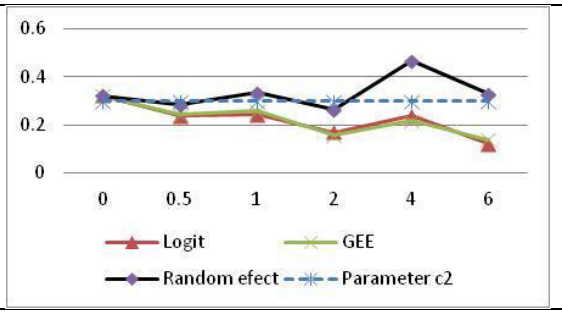

Figure 9. Estimator of γ_2

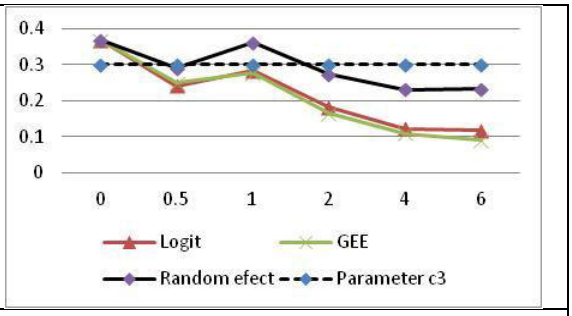

Figure 10. Estimator of γ_3

We can see that on $\sigma^2 = 0$ (no effect individual) estimators by three approximations are same. On general, estimator of independent Logit Model ($\hat{\theta}_{MLECS}$) and estimator of GEE ($\hat{\theta}_{GEE}$) are not different but increasing of σ^2 impact to increasing bias of estimator. On data having individual effect (see Figure 2 to Figure 10), the random effect model ($\hat{\theta}_{MLERE}$) better than $\hat{\theta}_{MLECS}$ and $\hat{\theta}_{GEE}$.

By GEE, we estimate coefficient regressions and correlation among alternative. Using effect random model we can estimate coefficient regressions, individual effect and covarians/correlations among alternative. On value of individual effect σ^2 about 1, random effect model can estimate covarians of utility more appropriate than the others value of σ^2.

5. Conclusion

On modelling binary panel response, we can use Random Effects Model. This model use the Extreme Value distribution and the standart normal distribution. The model is

$$P(y_{i1}, \ldots, y_{iT}) = \int_{-\infty}^{\infty} \prod_{t=1}^{T} (g_{it})^{y_{it}} (1 - g_{it})^{1-y_{it}} \phi(\alpha_i) d\alpha_i$$

with $g_{it} = \dfrac{\exp(V_{it} + \alpha_i)}{[1 + \exp(V_{it} + \alpha_i)]}$. The log-likelihood function is

$$\log L(\beta, \gamma, \sigma) = \sum_{i=1}^{n} \log\left(\int_{-\infty}^{\infty} \prod_{t=1}^{T} \left((g_{it})^{y_{it}} (1 - g_{it})^{1-y_{it}} \phi(\alpha_i) \right) \partial \alpha_i \right)$$

Based on simulation, Random Effects Model more appropriate than GEE.

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